

1. **(Hand this one in to David.)** Let  $t$  be Thomae's function defined on page 102. Prove that for any  $c \in [0, 1]$ ,  $\lim_{x \rightarrow c} t(x) = 0$ . Conclude that  $t$  is continuous at  $c$  if and only if  $c$  is irrational.
2. 3.3.1
3. 4.3.10
4. 4.4.3
5. Suppose  $f : \mathbb{R} \rightarrow \mathbb{R}$  and  $\lim_{x \rightarrow \infty} f(x) = 0$  and  $\lim_{x \rightarrow -\infty} f(x) = 0$ . Prove that  $f$  is bounded and attains either a minimum or a maximum. Give an example to show that  $f$  need not attain both a minimum and maximum.
6. 4.4.8
7. 4.5.3
8. 4.5.4
9. 4.5.6