

Determine the answers to the following questions in single elliptic and double elliptic geometry.

1. Given distinct points p and q , how many lines are on p and q ?
2. How long is a line?
3. If l and m are lines, do they intersect? How often?
4. In Euclidean geometry, a line divides all of space into two regions. How many regions does a line divide space into in single and double elliptic geometry?
5. Can a perpendicular to a line l always be drawn through a point p if p is on l ? If a perpendicular exists, is it unique?
6. Can a perpendicular to a line l always be drawn through a point p if p is not on l ? If a perpendicular exists, is it unique?
7. If k is a line and m and n are lines perpendicular to k , what can be said about the point of intersection of m and n ?
8. Can two lines have a common perpendicular? Can two lines have more than one common perpendicular? (Also, answer this question for Euclidean geometry).
9. Given a point p , a *polar* of p is a line k such that every line through p is perpendicular to k . Does every point p admit a polar? How many polars can a point p have?
10. What can be said about the angle sum of a triangle?
11. Euclid I-16 states that the exterior angle of a triangle is greater than either of the opposite interior angles. Show that Euclid I-16 is false in single and double elliptic geometry.