

1. Show that a countable product of sequentially compact spaces is sequentially compact.
2. Tychonoff's theorem implies  $[0, 1]^\omega$  is compact with the product topology and problem 1 implies it is sequentially compact as well. Determine if  $[0, 1]^\omega$  is compact or sequentially compact with the uniform and box topologies. The uniform topology on  $[0, 1]^\omega$  is given by the  $\ell^\infty$  metric:

$$d(x, y) = \sup_i |x_i - y_i|.$$

3: Munkres 51.2.

4: Munkres 51.3.

5: Munkres 52.1.