

1. Text 2.5. (Again) Present a (correct) triangulation, but **leave it to the reader to verify that it is a triangulation**. The reader will let you know if it is not correct. ☺ Prove that it is minimal by a solely combinatorial argument; see the hint in the book. Before using the hint, you must justify it (briefly).
  
2. (Euler characteristic of planar models, take 2) Let  $P$  be a standard  $n$ -gon (with  $n \geq 3$ ) (i.e. the polygon with vertices  $\exp(i\theta_k)$  with  $\theta_k = k/n$  for  $k = 0, 1, \dots, n-1$ ). Suppose we have a gluing scheme for the edges where each edge is glued to at most one other edge by means of an affine map. Let  $Q$  be the resulting quotient space, and let  $n_v$  and  $n_e$  be the number of vertices and edges respectively after identification.
  - a) Show by direct construction that  $Q$  can be triangulated.
  - b) Show that  $\chi(Q) = n_v - n_e + 1$ .
  - c) Compute the Euler characteristic of the torus, the Klein bottle, a sphere with 3 holes, the Möbius band, and a torus with a hole.
  
3. Identify the following surface:  $\langle a, b, c : abacb^{-1}c^{-1} \rangle$ .
  - a) Compute its Euler characteristic. (Use problem 2!)
  - b) Use cut/paste maneuvers to exhibit it as a connected sum of projective planes. Express your operations in terms of surface presentations.
  
4. People's choice. Go back and revisit any problem you received less than 6/10 (or equivalent) on. I'll upgrade your old assignment score, and you'll receive credit on the current assignment score, too.