

1. Working from the definition of continuity in a metric space, show that a function  $f : X \rightarrow Y$  is continuous at  $x \in X$  if and only if whenever  $(x_n)_{n=1}^{\infty}$  is a sequence in  $X$  converging to  $x$ ,  $(f(x_n))_{n=1}^{\infty}$  converges to  $f(x)$ .
2. Let  $(f_n)$  be a sequence of continuous functions from  $[0, 1]$  to  $\mathbb{R}$ . Suppose the sequence converges uniformly to a function  $f$ . Prove that  $f$  is continuous.
3. Carothers 1.26
4. Carothers 4.11
5. Carothers 4.14
6. Carothers 5.8
7. Carothers 5.17
8. Carothers 5.19
9. Carothers 5.24
10. Carothers 5.25
11. Carothers 5.26
12. Carothers 5.28